Reproducing works of Calder

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Many fine art pieces have been reproduced in digital form. The digital reproductions have been used to store and transmit the original work. In contrast, mobiles, or moving sculptures, such as those designed by Alexander Calder cannot be reproduced realistically by photographs and/or static images. The real characteristics of mobiles come from the motions generated by interactive external forces applied to their structures. Hence people could not fully enjoy them through static images or even static three-dimensional models. We present a virtual mobile system where users can easily control the mobile and can feel the impressions that the artist originally intended to provide. Virtual winds are generated by blowing on a microphone which then exert external forces to the mobile. This microphone interface lets users control the mobile while they are watching it through a monitor. We introduce a linear time solution for the constraint dynamics and an improved impulse dynamics to speed up the simulation. Using these techniques, we achieve a real-time simulation of the mobile on personal computers. The techniques presented can easily be extended to simulate other interactive dynamics systems. Copyright © 2001 John Wiley & Sons, Ltd.

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Introduction

Recently, real-world objects have been successfully reproduced in computer systems, using computer graphics and virtual reality techniques. A good application example is digital museums, which display reproductions of real-world fine art pieces on the computer. For drawings, digital scanners and/or digital cameras can be used to generate the digital reproductions. In the case of sculptures, three-dimensional geometric and/or volume data can be used to create virtual sculptures. Image-based rendering techniques including MCOP (multiple center of projection) can also be used for this purpose.

Mobiles, which are also known as moving sculptures, however, cannot be represented successfully using these techniques. As an example, a real-world mobile, ‘Steel Fish’ by Alexander Calder, is shown in Figure 1.

Figure 1. A real-world mobile: ‘Steel Fish’ by Alexander Calder.
due to external forces such as from winds. Much of people’s experience of the piece comes from real-time interactions with the piece.

In this paper, we present a physically based virtual mobile system. To simulate a real-world mobile, we start by constructing its geometric shape. Physical properties such as masses and inertia tensors are then calculated. The mobile is simulated by a constraint dynamics system based on these geometric data and physical properties. Users can generate virtual winds, and our constraint dynamics solver simulates the motions and collisions of the components. An impulse dynamics system is used to simulate collisions among the components of the mobile. Using a simplified aerodynamics model for the virtual wind and other acceleration techniques, our system accomplished real-time display of an example virtual mobile on Pentium chip-based personal computers. Although the system has value in reproducing mobiles, perhaps more importantly the techniques presented can be applied to other real-time physically based simulations.

The following sections describe the details of our virtual mobile system. In the next section, we present the overview of the system. The third section explains how virtual mobiles are constructed from the real-world mobiles. In the following three sections, the virtual wind model, the constraint dynamics solver, and the impulse dynamics solver are presented, respectively. Example sequences of animation are shown in the seventh section. Finally, conclusions and future work are given in the last section.

**System Overview**

Our system is implemented in the C++ programming language and OpenGL graphics library on Pentium chip-based PCs. Figure 2 is the block diagram of the system. At the pre-processing step, the system calculates geometric and physical properties of a virtual mobile. Initially, the mobile is in its equilibrium state. The user can generate virtual winds through the microphone interface and these virtual winds act as external forces. After finding the surfaces of the mobile influenced by the virtual wind, the forces applied on these surfaces are calculated.

Using these forces, our system simulates the motions of the mobile, using constraint dynamics and impulse dynamics techniques. The constraint forces due to the connectivity among the components are first calculated, and the constraint dynamics solver generates new positions. These new positions may cause collisions among the components of the mobile. After detecting the collisions, the impulse dynamics solver is used to handle these collisions. The system repeats
the above steps and displays the virtual mobile for each iteration.

**Data Acquisition**

To represent a virtual mobile, we need its geometric configurations and physical properties. It is, however, difficult to extract these properties from a real-world mobile. In this paper, we select ‘Steel Fish’ by A. Calder as an example, and reproduce its geometric configurations as shown in Figure 3.

The example consists of nine components, each of which acts as an independent motion unit (Figure 3(a)). Eight spherical joints with three degrees of freedom connect these components to each other (Figure 3(b)). From the dynamics point of view, these joints play the role of constraints.

For the dynamic simulation, the virtual mobile requires some physical parameters such as the mass, the location of the center of mass, and the inertia tensor for each component. Our system adjusts these parameters from the given geometric configurations to achieve equilibrium as shown in the original work.

Since the example has a tree-like shape, the mass ratios between components are computed in a bottom-up manner. As an example, the mass ratio between components $O_4$ and $O_5$ is calculated from the ratio of the length of $O_6^{left}$ and $O_6^{right}$ as shown in Figure 3(a). Notice that the geometric configuration only gives mass ratios. Hence the total mass of the mobile acts as a control parameter to finally calculate the mass of each component.

In addition to the mass of each component, we need to calculate the location of the center of mass and the inertia tensor. Assuming the components are uniform-density rigid bodies, these physical parameters are calculated in a straightforward manner. First, the volume of a component can be calculated from its geometric shape. From its mass and volume, the density of each component is specified. We then use Mirtich's integral equations to obtain other physical parameters. The geometric configurations and physical parameters are later used to simulate the dynamics behavior of the virtual mobile.

**Virtual Wind**

While natural wind causes the motion of real-world mobiles, we need virtual wind to simulate the motion of the virtual mobile. To control the virtual wind, we may use traditional input devices such as keyboards and mice. Additionally, our system uses a microphone interface. The user blows on the microphone, and the speed of the generated virtual wind is proportional to...
the amplitude of the input sound. The direction of the wind is specified with the mouse or stereo glasses with ultrasound head tracker.

The microphone interface has some benefits. First, it is more intuitive for the user to generate the wind through the blowing action. Second, the microphone is more convenient to simulate the temporal variations of the wind speed. Another benefit is that the microphone is inexpensive and easily available even for personal computers.

Since it is generated from the human breath, the virtual wind is assumed to propagate in an infinite cone shape, as shown in Figure 4. A circular cross-section $S_0$ with radius $r_0$ plays the role of the source of wind. The vertex of the cone is located at distance $l_0$ from the center of $S_0$. The user can provide $r_0$ and $l_0$ to control the shape of the cone, and the wind propagates from $S_0$ in the direction opposite to the vertex. Using the microphone interface, the user controls the wind speed $v_0(t)$ at $S_0$.

For simulating the wind, we need to calculate the speed of the wind at a distance $l_1 > l_0$ from the vertex. Although there are several results8–7 for simulating aerodynamics in computer graphics applications, we use a simplified form to achieve real-time display. We start with the assumption that the fluid (in this case, air) is not viscid and incompressible, and no fluid can cross the boundary of the cone shape. This is a reasonable model for air at normal speed.8 Then, the equation of continuity in fluid dynamics gives

$$A_0v_0 = A_1v_1 \tag{1}$$

where $A$ and $v$ represent the area of the cross-section and the fluid speed, respectively.8 The subscript $0$ and $1$ correspond to the distance $l_0$ and $l_1$, respectively.

From (1) and the geometric configurations of the cone, it is easily found that

$$\frac{v_1}{v_0} = \frac{A_0}{A_1} = \frac{\pi l_0^2}{\pi l_1^2} = \frac{r_0^2}{r_1^2} \tag{2}$$

Using the Stoke drag equation,8,9 the force acting on a face with its area $A$ located on the cross-section $S_1$ can be calculated as follows:

$$F_{\text{stoke}} = \rho A v_0^2 (\mathbf{n}_w \cdot \mathbf{n}_f) \mathbf{n}_f \tag{3}$$

where $\mathbf{n}_w$ and $\mathbf{n}_f$ are the unit directional vector of the wind and the face normal vector, respectively, as shown in Figure 5. The constant $\rho$ is the density of fluid. Equations (2) and (3) give

$$F_{\text{stoke}} = 2 \pi \frac{r_0^2}{l_1^2} (\mathbf{n}_w \cdot \mathbf{n}_f) \mathbf{n}_f$$

where $\mathbf{n}_w$ is the wind speed. Another benefit is that the microphone is inexpensive and easily available even for personal computers.

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where $\mathbf{n}_w$ is the wind speed.

Before applying the force calculated in (5) to the face, we should check whether the wind is directly delivered to the face or not. When a face is occluded by another face in the air flow, we simply assume that the occluded face is not influenced by the wind. Without this assumption, it is hard to achieve the real-time display of the mobile. In this simplified wind model, the air flow can reach the faces which are directly visible from the vertex of the cone and which belong to the interior of the cone.

The faces affected by the wind can be identified by a visible surface detection method. We use the depth-buffer method for more speed-up. To simulate the partially occluded cases, faces are first partitioned into small areas on which sampling points are assigned. The graphics pipeline is then used to capture the image containing the cross section $S_0$ using the synthetic camera located at the vertex of the cone. Each sampling point has its own identification number, and it is also stored in the alpha buffer through the graphics pipeline. Scanning the alpha buffer, we can easily detect whether each sampling point is visible from the vertex of the cone or not. Since $S_0$ corresponds to a circle on the image plane, it is also easy to check that the point belongs to the interior of the cone. When a sampling point is visible and also belongs to the interior of the cone, the force calculated in (5) is applied to its corresponding area. In the next section, we will present
Constraint Dynamics

Since the components of typical mobiles are connected with joints, constraint dynamics simulation is required to generate physically correct motions. In constraint dynamics simulation, two different methods are frequently used: the reduced coordinate method\(^\text{10}\) and Lagrange multiplier method.\(^\text{11,12}\) Although the reduced coordinate method can also be used, symbolic knowledge of the body-space to world-space mapping is required to parameterize the system’s degree of freedom.\(^\text{12}\) Our system is based on the Lagrange multiplier method. In this section, we will explain how the Lagrange multiplier method can be applied to the mobile. See References \(^\text{11}\) and \(^\text{12}\) for more details of the Lagrange multiplier method itself.

At each joint of the mobile, we need to apply constraint force to preserve connectivity due to the joint. Letting the position vectors of joints be \(q(t)\) at time \(t\), the Lagrange multiplier method calculates the constraint force \(Q = J^T \lambda\) by solving the following constraint force equation with respect to the Lagrange multiplier \(\lambda\):

\[
JWJ^T \lambda = -Jq - JWQ
\]  

(6)

where \(W\) is the inverse of generalized mass matrix and \(Q\) is externally applied force (virtual wind in this case). \(J\) is the Jacobian matrix \(\partial C/\partial q\) where the vector function \(C(q)\) is the concatenation of all constraint functions. After solving the above equation, the calculation of the constraint force \(Q\) is calculated in a straightforward manner.

Many numerical techniques can be used to solve the above equation.\(^\text{11–13}\) Among them, Baraff’s extension method\(^\text{12}\) gives linear time solutions for usual constraint functions. However, this method requires complicated algorithms for auxiliary constraints, which can frequently occur in the case of virtual mobiles. For chain-like objects, Surles presented a linear time solution through permutating the rows of the matrices.\(^\text{11}\) Our method is similar to Surles’ method. However, we avoid the permutation process through proper numbering of the constraints. This numbering can be performed as a pre-processing step, as shown in the following.

The joints in a mobile can be numbered in a bottom-up manner. Figure 3 shows the numbering of components and joints of our example mobile, ‘Steel Fish’. Notice that the component \(O_0\) is fixed to the ground and thus joint \(T_8\) act as a nail constraint while others act as point-to-point constraints. Using the bottom-up numbering of the joints, Jacobian matrix \(J\) in (6) can be expressed as

\[
J = \begin{bmatrix}
  j_{11} & j_{12} & & & & & & \\
  j_{22} & j_{23} & & & & & & \\
  j_{33} & & & & & & & \\
  j_{44} & j_{45} & & & & & & \\
  j_{55} & j_{56} & & & & & & \\
  j_{66} & j_{67} & & & & & & \\
  j_{77} & j_{78} & & & & & & \\
  j_{88} & & & & & & & \\
\end{bmatrix}
\]

where the denoted elements are constants and others are all zeros. The element \(j_{ij}\) is non-zero if and only if \(j_i\) connects the component \(O_j\) to another component. A tree-like object gives an upper triangular Jacobian matrix \(J\) with a bottom-up numbering of components and joints. Since \(J\) is upper triangular, the product of matrices \(JWJ^T\) in (6) can be expressed as

\[
JWJ^T = \begin{bmatrix}
  a_{11} & a_{12} & & & & & & \\
  a_{21} & a_{22} & a_{23} & & & & & \\
  a_{32} & a_{33} & & & & & & \\
  a_{44} & a_{45} & & & & & & \\
  a_{54} & a_{55} & a_{56} & & & & & \\
  a_{64} & a_{65} & a_{66} & & & & & \\
  a_{74} & a_{75} & a_{76} & a_{77} & a_{78} & & & \\
  a_{85} & a_{86} & a_{87} & a_{88} & & & & \\
\end{bmatrix}
\]

Letting the above matrix be \(A = [a_{ij}]\), we can easily find the following three characteristics:

1. diagonal elements \(a_{ii}\)’s are all non-zeros;
2. \(a_{ij}\) is non-zero if and only if \(a_{ji}\) is non-zero;
3. \(a_{ij}\) is non-zero if and only if a component is affected by both the \(i\)th and the \(j\)th constraints.

Although a few numerical methods can solve (6) in \(O(n)\) processing time, they are somewhat complex.\(^\text{11,12}\) In contrast, the above characteristics enable us to achieve the time complexity of \(O(n)\) even with the Gaussian elimination method, which is simple but requires \(O(n^3)\) time for general matrix equations.

During the Gaussian elimination process, we can always choose \(a_{ii}\) as the pivot element since all \(a_{ii}\)’s are non-zeros. When subtracting the \(i\)th row from the \(j\)th row with \(j > i\), no new non-zero elements in the \(j\)th row

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are introduced. The mobile has $O(n)$ constraints and thus the matrix $A = \mathbf{J} \mathbf{W} \mathbf{J}^T$ has only $O(n)$ non-zero elements. Therefore, we need only $O(n)$ operations for the matrix solution, to finally achieve the linear-time solutions for our constraint-dynamics model.

**Collision Handling**

When simulating the motion of mobiles with constraint dynamics, collisions between its components will necessarily happen. Although there are many general collision detection methods,\textsuperscript{14,15} collision detection can be achieved more efficiently through analyzing the characteristics of the mobile. First, some pairs of the components cannot collide with each other. As an example, the components $O_3$ and $O_5$ can never collide with each other in our example mobile. A pre-processing step detects all such pairs of components so that they can be excluded from the collision detection process. Additionally, some components are simple geometric shapes such as cylinders and spheres. Thus, we can use cylinder-to-cylinder, cylinder-to-sphere, and sphere-to-sphere collision detection methods, which are much faster than the usual polyhedron-to-polyhedron collision detection methods.

After detecting collisions, we use the impulse-based collision response method.\textsuperscript{16,17} Since this method can calculate the new velocities instantaneously, it is suitable for real-time applications. The penalty method,\textsuperscript{17} which is also widely used in the collision response, requires small time steps for accurate simulation, and is not appropriate for real-time applications.

In the case of a mobile, the collision response method should cooperate with the constraint dynamics model. Thus, the constraints at the joints and frictions at the collision points should also be handled during the collision response. Moore formulated the impulse equations for articulated figures, and his equation can be used for joint constraints.\textsuperscript{17}

Letting the components of the mobile be $O_i$, $1 \leq i \leq n$, the mass and inertia tensor of $O_i$ is denoted as $m_i$ and $I_i$, respectively. Due to the collision, the linear and angular velocity of $O_i$ may be changed. Let $\mathbf{v}_i$ and $\mathbf{w}_i$ be the linear and angular velocity of $O_i$ with respect to the center of mass of $O_i$ before the collision. The impulse-based collision response method aims to calculate the linear velocity $\mathbf{v}_i$ and the angular velocity $\mathbf{w}_i$ of $O_i$ after the collision.

The impulse-based collision response method starts from the law of momentum conservation. Since the change of momentum before and after the collision equals to the sum of impulses at the time of collision, the impulse equations for $O_i$ can be expressed as follows:

$$m_i(\mathbf{v}_i - \mathbf{v}_i) = \mathbf{P} + \sum_j \mathbf{P}_{ij}$$

and

$$I_i(\mathbf{w}_i - \mathbf{w}_i) = \mathbf{I}_i \times \mathbf{P} + \sum_j \mathbf{l}_{ij} \times \mathbf{P}_{ij}$$

where $\mathbf{P}$ is the impulse applied to $O_i$ and $\mathbf{P}_{ij}$ is the attachment impulse on $O_i$ due to $O_j$, which is connected to $O_i$ using a joint constraint. When $O_i$ and $O_j$ are not directly connected to each other, $\mathbf{P}_{ij}$ is a null vector. Notice that $\mathbf{P}$ can be zero for non-colliding components. The vectors $\mathbf{I}_i$ and $\mathbf{l}_{ij}$ are the distance vectors from the center of mass of $O_i$ to the collision point and to the joint connecting $O_i$ and $O_j$, respectively, as shown in Figure 6.

Joint constraints also give additional equations. When a spherical joint connects $O_i$ and $O_j$, their relative velocity at the contact point should be equal to each other:

$$\mathbf{v}_i + \mathbf{w}_i \times \mathbf{l}_{ij} = \mathbf{v}_j + \mathbf{w}_j \times \mathbf{l}_{ij}.$$ 

In the case of nail constraints, a point on the component $O_k$ has a fixed position. Thus, the linear velocity of the nailed point is zero:

$$\mathbf{v}_k + \mathbf{w}_k \times \mathbf{l}_{ik} = 0$$

where $\mathbf{l}_{ik}$ is the vector from the center of mass of $O_k$ to the nailed point.

Moore extended this formulation to cases with

![Figure 6. Impulse-based collision response.](image-url)
friction. However, this requires solving the whole systems of linear equations repeatedly to determine the friction status of each collision point. We improve this method by combining it with Mirtich’s conditional equation for friction.15

When a point of $O_i$ is colliding with a face of $O_j$, the plane containing that face is defined as the collision plane, as shown in Figure 7. With respect to the normal vector $N$ of the collision plane, the impulse $P$ for $O_i$ can be divided into two components: the normal component $P_N$ and the tangential component $P_T = P - P_N$. The state of friction can be classified into two cases: sticking case and sliding case. From the viewpoint of impulse, the sticking case means there is no slip at the collision point, which satisfies the condition $|P_T| \leq \mu |P_N|$ with the friction coefficient $\mu$. When $|P_T| > \mu |P_N|$, the collision point will slip along the collision plane and it is the sliding case.

Since the sliding and sticking cases result in different equations, it is important to identify whether a collision point is sticking or sliding. For sticking cases, the collision point does not move along the collision plane. In contrast, the friction force will act on the sliding collision points.

Using Moore’s formulation, it is impossible to decide whether a collision point is sliding or sticking without calculating the impulse. Mirtich introduced a prediction equation for sliding conditions.15 The friction at a collision point is sliding when it satisfies the following condition:

$$\left(\frac{1}{k_{11}}\right)^2 + \left(\frac{1}{k_{23}}\right)^2 > \mu^2 \left(\frac{1}{k_{33}}\right)^2$$

where the $3 \times 3$ matrix $K = [k_{ij}]$ is equal to $(1/m_i + 1/m_j)E - (I_i \times I_j^{-1})^{-1}I_i + I_j \times I_j^{-1}$ with the $3 \times 3$ identity matrix $E$. We use this prediction equation to speed up the impulse calculation.

**Figure 7. Collision plane.**

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**Example**

Our example, ‘Steel Fish’, has nine components connected by eight joints. Our constraint dynamics solver uses a total of 24 constraint functions for the three directions of the eight joints. Thus, we need to solve the $24 \times 24$ matrix equation to obtain the constraint forces.

For the dynamics-based simulation, we should calculate linear velocities and angular velocities of eight components excluding the fixed component $O_0$. Using impulse-based collision handling, we also need to calculate the impulse $P$ and the attachment impulses $P_i$’s of the eight joints. Thus, the number of unknowns is 81, and the impulse dynamics solver needs to solve the $81 \times 81$ matrix equation.

An example sequence of images generated by our virtual mobile system is shown in Figure 8. Our system was executed on a personal computer with a 350 MHz Pentium chip and 64 Mbytes of main memory. We use software-implemented OpenGL libraries for rendering, without any hardware acceleration. The simplified virtual wind model and customized dynamics solvers enable us to simulate the example mobile interactively. Figure 9 shows another sequence of images for the mobile named ‘Southern Cross’, which was also originally created by A. Calder.

**Conclusion**

Our aim was to reproduce a real-world mobile on a low-end computer system. To achieve this goal, we developed a dynamics-based virtual mobile system. To interactively display the virtual mobile, our system concentrates on three improvements: the virtual wind model, constraint dynamics solver, and the impulse dynamics solver.

First, we suggested a wind model, which is simple but sufficient to simulate directional winds. Additionally, the microphone interface is developed for easy control of the virtual wind. Since this wind model can generate directional winds, it is suitable for simulating artificial winds generated by electric fans, air-conditioners, etc. Future work will include improving our wind model by combination with existing natural wind models.

As a dynamics system, our virtual mobile system uses a constraint dynamics solver and an impulse
Figure 8. Example sequences of images.
Figure 9. Another example sequences of images.
dynamics solver. For real-time display, both are highly tuned for simulating typical mobiles. Since usual mobiles are tree-like shapes, this improvement can also be used for general tree-like objects.

The specific real example of the mobile allowed us to focus on technical problems. While such systems have inherent value, perhaps more important is the fact that the improvements that have been made to existing techniques can be used to simulate other real-time systems.

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References


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